# Discussion of "Investment Opportunities and the Sources of Lifetime Inequality" by Athreya, lonescu, Neelakantan, and Vidangos 

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## Brief Summary

- Given the initial inequality, explore the determination of lifetime inequality in a PE quantitative life-cycle model
- Conditional on (not) having the access to two investment opportunities

1. college education
2. stock market investment

- Questions

1. source of lifetime inequality? initial variance vs. over-time earning dynamics
2. role for each investment opportunity?

- Answers

1. initial variance ( $70 \%$ for lifetime earning inequality and $76 \%$ for wealth inequality)
2. college education option $\Uparrow$ inequality \& stock investment option slightly $\Downarrow$ inequality

## Model Overview

Time Line: Individuals' Life-cycle


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- shocks to an agent's effective wage: $z_{i, t} h_{t} w_{t}\left(1-l_{t}\right)$
- shocks to excess return of equity investment: $\tilde{R}_{t}=\mu+\eta_{t}$


## Inspecting the Key Mechanisms

- College Education
- $\Leftrightarrow$ option to accumulate human capital when young and cheaper

1. delay building $h$ incurs greater opportunity cost when working for $w_{t}=\left(1+g_{i}\right)^{t-1}$
2. "trend gain" for college graduates: $g_{c g}>g_{n c}$

- risk: low type a and low $h_{0}$ may fail to complete college for $\pi^{\prime}(a \mid)>$.0 and $\pi^{\prime}\left(h_{0} \mid.\right)>0$
- risk + wealth-poor given college fee: less likely to enroll


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1. All agents may quickly build human capital to optimal size of $h$ when young $\Rightarrow \downarrow$ inequality of $h$ and earnings
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## Inspecting the Key Mechanisms (Cont.)

- Stock Investment
- Can happen at any stage $t$ of life
- portfolio choice: wealth to stock, risk-free asset, and consume
- interaction with college education: (high) low a and $h_{0} \Rightarrow$ (less) more likely to participate in stock investment


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1. high type $a, h_{0}, x_{0}$ are wealth-rich and get richer $\Rightarrow \uparrow$ inequality
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1. high type $a, h_{0}, x_{0}$ are wealth-rich and get richer $\Rightarrow \uparrow$ inequality
2. b/c college investment option, low type agents may lift off earlier in life via stock investment $\Rightarrow \downarrow$ inequality (Effect 2 dominates: $\Downarrow$ )

## Comments

- A very interesting paper with a really nice framework relative to e.g. (Huggett et al., AER 2011):
- building $h$ in college paying a fixed cost (college fee) under completion risk vs. working-life accumulation
- Investor sophistication link to stock investment performance?
- e.g. evidence and theory in Kacperczyk, Nosal and Stevens (2014)
- may attenuate the Effect 2 (stock) and reinforce the Effect 2 (college)
- or, some fixed cost of entering the stock market may do
- What if the student loan is defaultable? or if the repayment schedule is not linear in time, e.g. a fraction of realized wage level after college?
- wealth effect may encourage both college and stock market participation?


## Some Data on Student Loan Defaults

## Default Rates

Two-Year Cohort Default Rate
Calculated based on BORROWERS and the two-year window after entering repayment. Cohort is based on fiscal year.

| Institutional Category |  | Cohort Yr 2008 Cohort Default Rate (CDR)\% | Cohort Yr 2009 <br> Cohort Default Rate (CDR)\% | Cohort Yr 2010 <br> Cohort Default Rate (CDR)\% | Cohort Yr 2011 <br> Cohort Default Rate (CDR)\% |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Public |  |  |  |  |  |
| Less than 2 Yrs | 7.5\% | 6.7\% | 9.9\% | 10.0\% | 9.3\% |
| 2-3 Yrs | 9.9\% | 10.1\% | 11.9\% | 13.4\% | 15.0\% |
| 4 yrs + | 4.3\% | 4.4\% | 5.2\% | 6.0\% | 6.8\% |
| Private Non-Profit |  |  |  |  |  |
| Less than 2 Yrs | 12.6\% | 14.1\% | 14.5\% | 13.6\% | 14.0\% |
| 2-3 Yrs | 8.1\% | 8.2\% | 10.0\% | 8.5\% | 8.2\% |
| 4 yrs + | 3.6\% | 3.8\% | 4.5\% | 5.1\% | 5.1\% |
| Proprietary |  |  |  |  |  |
| Less than 2 Yrs | 12.0\% | 12.4\% | 13.7\% | 11.8\% | 14.1\% |
| 2-3 Yrs | 12.5\% | 12.6\% | 14.8\% | 12.0\% | 13.9\% |
| $4 \mathrm{yrs}+$ | 9.8\% | 10.9\% | 15.4\% | 13.6\% | 13.4\% |
| Foreign Schools | 2.2\% | 2.2\% | 5.5\% | 2.9\% | 2.7\% |
|  |  |  |  |  |  |
| Overall | 6.7\% | 7.0\% | 8.8\% | 9.1\% | 10.0\% |

Source: U.S. Department of Education, Office of Federal Student Aid

## Some Data on Repayment Plan

## Snapshot: Direct Loan and FFEL Program Repayment Plans

| Extended <br> Repayment Plan | - Direct Subsidized and Unsubsidized Loans <br> - Subsidized and Unsubsidized Federal Stafford Loans <br> - all PLUS loans <br> - all Consolidation Loans (Direct or FFEL) | Payments may be fixed or graduated. <br> Up to 25 years. | - If you're a Direct Loan borrower, you must have more than $\$ 30,000$ in outstanding Direct Loans. <br> - If you're a FFEL borrower, you must have more than $\$ 30,000$ in outstanding FFEL Program loans. <br> - Your monthly payments will be lower than under the 10 -year Standard Plan or the Graduated Repayment Plan. <br> - You'll pay more over time than under the 10 -year Standard Plan. |
| :---: | :---: | :---: | :---: |
| Revised Pay As You <br> Earn Repayment <br> Plan (REPAYE) | - Direct Subsidized and Unsubsidized Loans <br> - Direct PLUS loans made to students <br> - Direct Consolidation Loans that do not include PLUS loans (Direct or FFEL) made to parents | - Your monthly payments will be 10 percent of discretionary income. <br> - Payments are recalculated each year and are based on your updated income and family size. <br> - If you're married, both your and your spouse's income or loan debt will be considered, whether taxes are filed jointly or separately (with limited exceptions). <br> - Any outstanding balance on your loan will be forgiven if you haven't repaid your loan in full after 20 or 25 years. | - Any Direct Loan borrower with an eligible loan type may choose this plan. <br> - Your monthly payment can be more than the 10 year Standard Plan amount. <br> - You may have to pay income tax on any amount that is forgiven. <br> - Good option for those seeking Public Service Loan Forgiveness (PSLF). |
| Pay As You Earn Repayment Plan (PAYE) | - Direct Subsidized and Unsubsidized Loans <br> - Direct PLUS loans made to students <br> - Direct Consolidation Loans that do not include (Direct or FFEL) PLUS loans made to parents | - Your maximum monthly payments will be 10 percent of discretionary income. <br> - Payments are recalculated each year and are based on your updated income and family size. <br> - If you're married, your spouse's income or loan debt will be considered only if you file a joint tax return. <br> - Any outstanding balance on your loan will be forgiven if you haven't repaid your loan in full after 20 years. | - You must be a new borrower on or after Oct. 1, 2007, and must have received a disbursement of a Direct Loan on or after Oct. 1, 2011. <br> - You must have a high debt relative to your income. <br> - Your monthly payment will never be more than the 10 -year Standard Plan amount. <br> - You'll pay more over time than under the 10 -year Standard Plan. <br> - You may have to pay income tax on any amount that is forgiven. <br> - Good option for those seeking Public Service Loan Forgiveness (PSLF). |

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## Something More

- Paper assumes away the selection mechanism of the college admission. - selecting the high type a and $h_{0}$ at $t=0$ is equivalent to expecting a completion risk at $t=4$ ?
- Some room for improving the calibration: over-predicting the mean earnings for seniors above 55 , due to the excessive exposure to stock market investments?
- some empirical testings? elasticity of stock market participation (fraction among the cohorts \& the size of investment quantity) w.r.t. inequality?


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- some empirical testings? elasticity of stock market participation (fraction among the cohorts \& the size of investment quantity) w.r.t. inequality?
- a great paper!

Thank You Very Much!

